SAMPLE OUESTION OAPER

BLUE PRINT

Time Allowed : 3 hours

Maximum Marks: 80

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S. No.	Chapter	VSA/Case based (1 mark)	SA-I (2 marks)	SA-II (3 marks)	LA (5 marks)	Total
1.	Relations and Functions	3(3)	_	1(3)	-	4(6)
2.	Inverse Trigonometric Functions	_	1(2)	_	-	1(2)
3.	Matrices	2(2)#	1(2)*	-	-	3(4)
4.	Determinants	1(1)	_	_	1(5)*	2(6)
5.	Continuity and Differentiability	1(1)	1(2)*	2(6)#	-	4(9)
6.	Application of Derivatives	1(1)*	2(4)	1(3)*	-	4(8)
7.	Integrals	2(2)#	1(2)*	1(3)	-	4(7)
8.	Application of Integrals	-	1(2)	1(3)	_	2(5)
9.	Differential Equations	1(1)	1(2)	1(3)	_	3(6)
10.	Vector Algebra	3(3)#	_	_	_	3(3)
11.	Three Dimensional Geometry	1(4)	1(2)	_	1(5)*	3(11)
12.	Linear Programming	-	_	-	1(5)*	1(5)
13.	Probability	2(2)# + 1(4)	1(2)	-	_	4(8)
	Total	18(24)	10(20)	7(21)	3(15)	38(80)

*It is a choice based question.

[#]Out of the two or more questions, one/two question(s) is/are choice based.

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Subject Code : 041

MATHEMATICS

Time allowed : 3 hours

General Instructions :

- 1. This question paper contains two parts A and B. Each part is compulsory. Part-A carries 24 marks and Part-B carries 56 marks.
- 2. Part-A has Objective Type Questions and Part-B has Descriptive Type Questions.
- Both Part-A and Part-B have internal choices. 3.

Part - A :

- 1. It consists of two Sections-I and II.
- 2. Section-I comprises of 16 very short answer type questions.
- 3. Section-II contains 2 case study-based questions.

Part - B:

- It consists of three Sections-III, IV and V. 1.
- 2. Section-III comprises of 10 questions of 2 marks each.
- Section-IV comprises of 7 questions of 3 marks each. 3.
- Section-V comprises of 3 questions of 5 marks each. 4.
- Internal choice is provided in 3 questions of Section-III, 2 questions of Section-IV and 3 questions of Section-V. 5. You have to attempt only one of the alternatives in all such questions.

PART - A

Section - I

1. Suppose *P* and *Q* are two different matrices of order $3 \times n$ and $n \times p$, then find the order of the matrix $P \times Q$.

OR

Simplify: $\begin{bmatrix} 7 & 1 & 2 \\ 9 & 2 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix} + 2 \begin{bmatrix} 4 \\ 2 \end{bmatrix}$

2. Write the general solution of differential equation $\frac{dy}{dx} = e^{x+y}$.

3. Prove that the function $f(x) = \log(1+x) - \frac{2x}{2+x}$ is increasing on $(-1, \infty)$.

Find the equation of the tangent to the curve $y^2 = 4ax$ at the point $(at^2, 2at)$.

4. Let $A = \{a, b, c\}$ and *R* be the relation defined on *A* as follows : $R = \{(a, a), (b, c), (a, b)\}.$

Write minimum number of ordered pairs to be added to R to make R reflexive and transitive.

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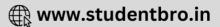
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Maximum marks : 80

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5. Evaluate :
$$\int \frac{x^3 - x^2 + x - 1}{x - 1} dx$$

Evaluate : $\int (4x^3 + 3x^2 + 2x + 4)dx$

- 6. If $\begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$, then find the value of *y*.
- 7. If α , β , γ are the direction angles of a vector and $\cos \alpha = \frac{14}{15}$, $\cos \beta = \frac{1}{3}$, then find $\cos \gamma$.
- 8. Find the area of the parallelogram whose adjacent sides are $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$ and $\vec{b} = 3\hat{i} 2\hat{j} + \hat{k}$.

OR

If \vec{a} and \vec{b} are two vectors such that $|\vec{a}| = 10$, $|\vec{b}| = 15$ and $\vec{a} \cdot \vec{b} = 75\sqrt{2}$, then find the angle between \vec{a} and \vec{b} .

9. Two cards are drawn at random and one-by-one without replacement from a well-shuffled pack of 52 playing cards. Find the probability that one card is red and the other is black.

OR

When will be two events A and B independent?

- **10.** Find the derivative of $(4x^3 5x^2 + 1)^4$ w.r.t. to *x*.
- **11.** Show that the relation *R* on the set $\{1, 2, 3\}$ given by $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3)\}$ is reflexive but neither transitive nor symmetric.
- 12. Find the value of $\int_{0}^{2\pi} |\sin x| dx$.
- **13.** Using determinants, find the area of triangle with vertices (2, -7), (1, 3), (10, 8).
- 14. If $|\vec{a} \times \vec{b}|^2 + |\vec{a} \cdot \vec{b}|^2 = 400$ and $|\vec{a}| = 5$, then write the value of $|\vec{b}|$.
- **15.** Four cards are drawn successively without replacement from a deck of 52 cards. Find the probability that all the four cards are king.
- **16.** If f(x) = [|x|], where $[\cdot]$ is the greatest integer function, then find f(-5/4).

Section - II

Case study-based questions are compulsory. Attempt any 4 sub parts from each question. Each sub-part carries 1 mark.

17. Suppose you visit to a hotel with your family and you observe that floor of a hotel is made up of mirror polished Kota stone. Also, there is a large crystal chandelier attached at the ceiling of the hotel. Consider the floor of the hotel as a plane having equation 3x - y + 4z = 2 and crystal chandelier as the point (3, -2, 1).



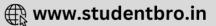
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OR

Based on the above information, answer the following questions:

- (i) The d.r.'s of the perpendicular from the point (3, -2, 1) to the plane 3x y + 4z = 2, is
- (a) <3, 1, 4 > (b) <3, -1, 4 > (c) <4, 1, 3 > (d) <4, -1, 3 > (i) The length of the perpendicular from the point (3, -2, 1) to the plane 3x y + 4z = 2, is

(a)
$$\sqrt{13}$$
 units (b) $\frac{1}{2}\sqrt{13}$ units (c) $\sqrt{\frac{13}{2}}$ units (d) $\frac{13}{\sqrt{2}}$ units

(iii) The equation of the perpendicular from the point (3, -2, 1) to the plane 3x - y + 4z = 2, is

(a)
$$\frac{x-3}{3} = \frac{y-2}{-1} = \frac{z-1}{4}$$
 (b) $\frac{x-3}{3} = \frac{y+2}{-1} = \frac{z-1}{4}$ (c) $\frac{x+3}{3} = \frac{y+2}{-1} = \frac{z-1}{4}$ (d) None of these (iv) The foot of the perpendicular drawn from the point (3, -2, 1) to the plane $3x - y + 4z = 2$, is

(a)
$$\left(\frac{3}{2}, \frac{-3}{2}, -1\right)$$
 (b) $\left(\frac{-3}{2}, \frac{3}{2}, -1\right)$ (c) $\left(\frac{3}{2}, \frac{3}{2}, -1\right)$ (d) $\left(\frac{1}{2}, \frac{3}{2}, -1\right)$
(v) The image of the point (3, -2, 1) in the given plane is

- (a) (0, 1, 3) (b) (0, -1, 3) (c) (0, 1, -3) (d) (0, -1, -3)
- **18.** A factory has three machines *A*, *B* and *C* to manufacture bulbs. Machine *A* manufacture 25%, machine *B* manufacture 35% and machine *C* manufacture 40% of the bulbs respectively. Out of their respective outputs 5%, 4% and 2% are defective. A bulb is drawn at random from total production and it is found to be defective.



Based on the above information, answer the following questions :

(i) Probability that defective bulb drawn is manufactured by machine *A*, is

(a)
$$\frac{41}{69}$$
 (b) $\frac{25}{69}$ (c) $\frac{16}{69}$ (d) $\frac{69}{2000}$
(ii) Probability that defective bulb drawn is manufactured by machine *B*, is

(iii) Probability that defective bulb drawn is manufactured by machine *C*, is

(a)
$$\frac{16}{69}$$
 (b) $\frac{17}{69}$ (c) $\frac{25}{69}$ (d) $\frac{42}{49}$

(iv) Probability that defective bulb is not manufactured by machine *B*, is

(a)
$$\frac{2}{69}$$
 (b) $\frac{61}{69}$ (c) $\frac{41}{69}$ (d) $\frac{1}{7}$

(v) If a bulb is drawn at random, then what is the probability that bulb drawn is defective ?
(a) 0.03
(b) 0.09
(c) 0.3
(d) 0.9

PART – B

Section - III

19. If
$$\sin^{-1}x + \sin^{-1}y + \sin^{-1}z = \frac{3\pi}{2}$$
, then find the value of $x^2 + y^2 + z^2 + 2xyz$.

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20. The equation of the line in vector form passing through the point (-1, 3, 5) and parallel to line $\frac{x-3}{2} = \frac{y-4}{3}, z = 2$.

21. Discuss the continuity of the function f(x) at $x = \frac{1}{2}$, when f(x) is defined as follows:

$$f(x) = \begin{cases} \frac{1}{2} + x, & 0 \le x < \frac{1}{2} \\ 1, & x = \frac{1}{2} \\ \frac{3}{2} + x, & \frac{1}{2} < x \le 1 \end{cases}$$

OR

If
$$y = ae^{2x} + be^{-x}$$
, then show that $\frac{d^2y}{dx^2} - \frac{dy}{dx} - 2y = 0$.

- **22.** Solve the differential equation $xe^{-y} dx + y dy = 0$.
- **23.** Evaluate : $\int (1-x)(2+3x)(5-4x) dx$

OR

Evaluate :
$$\int \frac{1}{x^2 + 2x + 10} dx$$

- **24.** Find the maximum value of slope of the curve $y = -x^3 + 3x^2 + 12x 5$.
- **25.** Find the points on the curve $y = x^3 3x^2 4x$ at which the tangent lines are parallel to the line 4x + y 3 = 0.
- **26.** Find the area enclosed between the curve $y = \sqrt{x-1}$, the *x*-axis and the line x = 5.
- 27. Urn 1 contains 5 white balls and 7 black balls. Urn 2 contains 3 white and 12 black balls. A fair coin is flipped, if it is head, a ball is drawn from Urn 1, and if it is tail, a ball is drawn from Urn 2. Suppose that this experiment is done and a white ball was selected. What is the probability that this ball was in fact taken from Urn 2?

28. If $\begin{bmatrix} 2x & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ -3 & 0 \end{bmatrix} \begin{bmatrix} x \\ 3 \end{bmatrix} = 0$, then find x. Show that $AB \neq BA$, where $A = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$

Section - IV

29. Solve the differential equation : $\frac{dy}{dx} + y \sec^2 x = \tan x \sec^2 x$; y(0) = 1**30.** Evaluate : $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$

31. For what choices of *a* and *b*, the function $f(x) = \begin{cases} x^2, & x \le c \\ ax+b, & x > c \end{cases}$ is differentiable at x = c? OR

Differentiate $(e^x \cos^3 x \sin^2 x)$ w.r.t. *x*.

32. Let $f: R \to R$ be defined by f(x) = x + |x|. Show that *f* is neither one-one nor onto.

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33. Find the area enclosed between the circle $x^2 + y^2 = 1$ and the line x + y = 1 lying in the first quadrant.

34. Find the equation of the normal to the curve $y = 2 \sin^2 3x$ at $x = \frac{\pi}{6}$.

OR

Find the values of *x* for which the function $f(x) = x^3 + 12x^2 + 36x + 6$ is decreasing.

35. If $f(x) = \begin{cases} mx+1, & \text{if } x \le \frac{\pi}{2} \\ \sin x + n, & \text{if } x > \frac{\pi}{2} \end{cases}$ is continuous at $x = \frac{\pi}{2}$, then find the relation between *m* and *n*.

Section - V

36. Use product $\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{bmatrix} \begin{bmatrix} -2 & 0 & 1 \\ 9 & 2 & -3 \\ 6 & 1 & -2 \end{bmatrix}$ to solve the system of equations x + 3z = 9, -x + 2y - 2z = 4, 2x - 3y + 4z = -3.

OR

If $A = \begin{bmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{bmatrix}$, then find $A^2 - 5A + 4I$ and hence find a matrix X such that $X = 5A - 4I - A^2$.

37. Solve the following problem graphically.

Minimize $Z = \frac{1}{1000} (1800000 + 30x - 30y)$ subject to constraints: $0 \le x \le 15000$ $0 \le y \le 20000$ $15000 \le x + y \le 30000$

OR

Solve the following problem graphically. Maximize Z = x + ysubject to constraints: $2x + 5y \le 100$ $\frac{x}{25} + \frac{y}{40} \le 1$ $x, y \ge 100$

38. Find the vector equation of the plane passing through the intersection of the planes $\vec{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 6$ and $\vec{r} \cdot (\hat{2i} + \hat{3j} + 4\hat{k}) = -5$ and the point (1, 1, 1).

OR

Find the vector and cartesian forms of the equation of the plane passing through the point (1, 2, -4) and parallel to the lines $\vec{r} = \hat{i} + 2\hat{j} - 4\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$ and $\vec{r} = \hat{i} - 3\hat{j} + 5\hat{k} + \mu(\hat{i} + \hat{j} - \hat{k})$.

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